

Policy

Calculation & Maths

2023-24

Mission Statement

The Members of the Community of St Joan of Arc School, by respecting each other, learn and grow in the love of Christ.

Rationale

This policy outlines a progression through written strategies for addition, subtraction, multiplication and division in line with the new National Curriculum commencing September 2014. Through the policy, we aim to link key manipulatives and representations in order that the children can be vertically accelerated through each strand of calculation. We know that school wide policies, such as this, can ensure consistency of approach, enabling children to progress stage by stage through models and representations they recognise from previous teaching, allowing for deeper conceptual understanding and fluency. As children move at the pace appropriate to them, teachers will be presenting strategies and equipment appropriate to children's level of understanding. However, it is expected that the majority of children in each class will be working at age-appropriate levels as set out in the National Curriculum 2014 and in line with school policy.

The importance of mental mathematics

While this policy focuses on written calculations in mathematics, we recognise the importance of the mental strategies and known facts that form the basis of all calculations. The following checklists outline the key skills and number facts that children are expected to develop throughout the school.

To add and subtract successfully, children should be able to:

- recall all addition pairs to 9 + 9 and number bonds to 10
- recognise addition and subtraction as inverse operations
- add mentally a series of one digit numbers (e.g. 5 + 8 + 4)
- add and subtract multiples of 10 or 100 using the related addition fact and their knowledge of place value (e.g. 600 + 700, 160 — 70)
- partition 2 and 3 digit numbers into multiples of 100, 10 and 1 in different ways (e.g. partition 74 into 70 + 4 or 60 + 14)
- use estimation by rounding to check answers are reasonable
- .

To multiply and divide successfully, children should be able to:

- · add and subtract accurately and efficiently
- recall multiplication facts to $12 \times 12 = 144$ and division facts to $144 \div 12 = 12$
- use multiplication and division facts to estimate how many times one number divides into another etc.
- know the outcome of multiplying by 0 and by 1 and of dividing by 1
- understand the effect of multiplying and dividing whole numbers by 10, 100 and later 1000
- recognise factor pairs of numbers (e.g. that $15 = 3 \times 5$, or that $40 = 10 \times 4$) and increasingly able to recognise common factors
- derive other results from multiplication and division facts and multiplication and division by 10 or 100 (and later 1000)
- notice and recall with increasing fluency inverse facts

- partition numbers into 100s, 10s and 1s or multiple groupings
- understand how the principles of commutative, associative and distributive laws apply or do not apply to multiplication and division
- understand the effects of scaling by whole numbers and decimal numbers or fractions
- · understand correspondence where n objects are related to m objects
- investigate and learn rules for divisibility

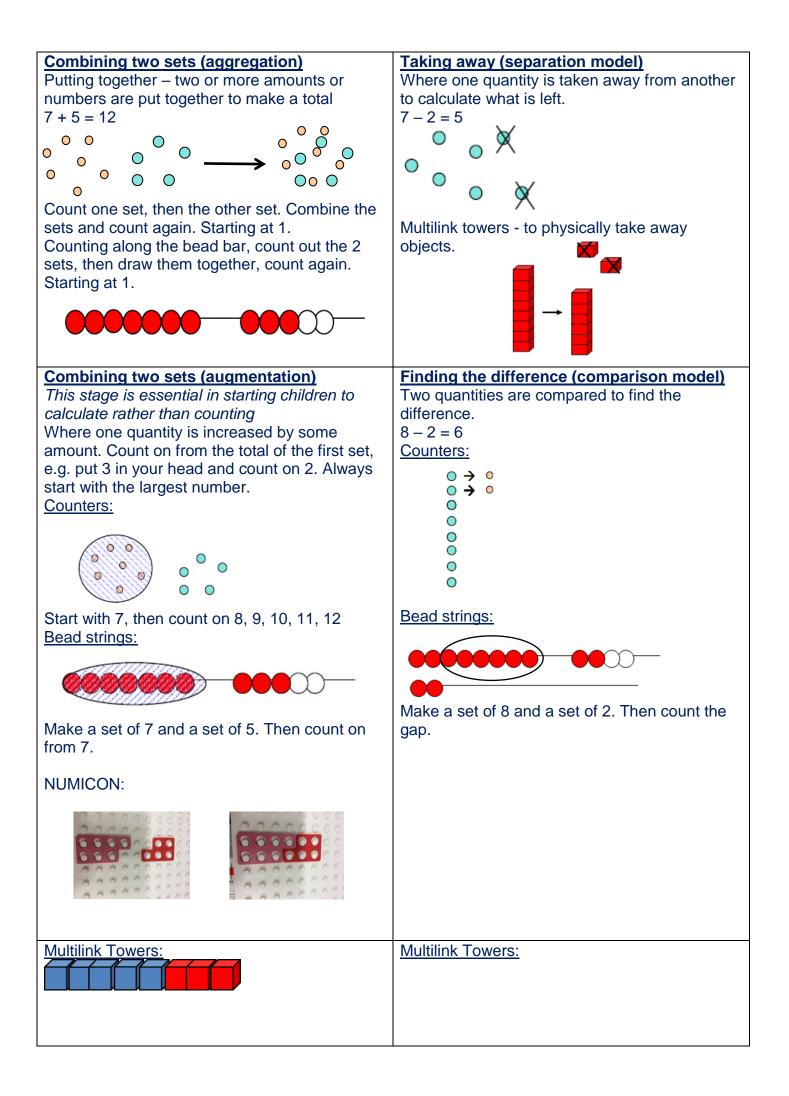
Progression in addition and subtraction

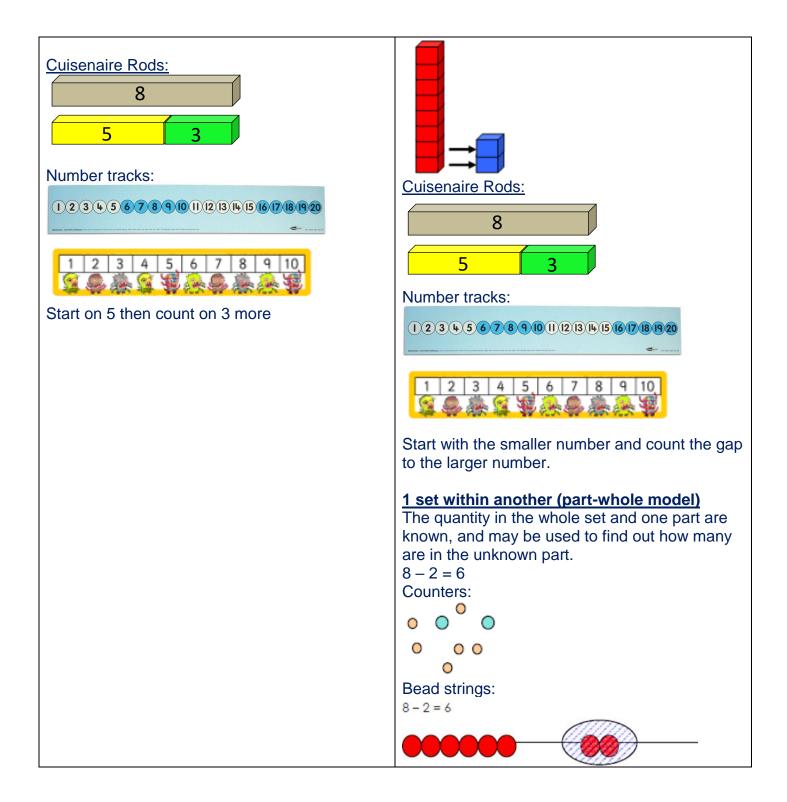
Addition and subtraction are connected.

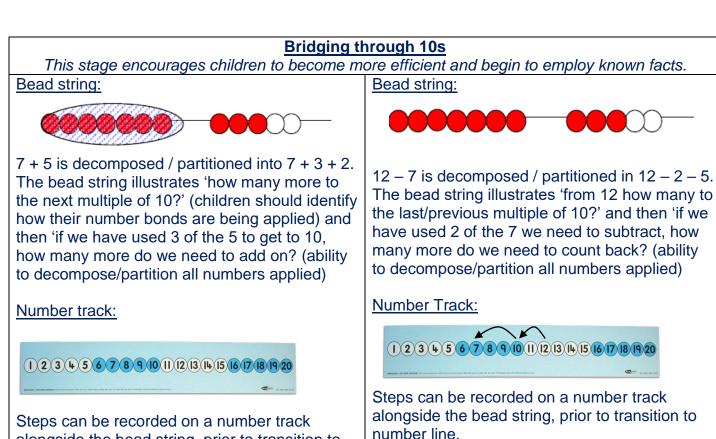
| Part | Part |
|-------|------|
| Whole | |

Addition names the whole in terms of the parts and subtraction names a missing part of the whole.

| Addition | Subtraction |
|----------|-------------|
| Addition | Subtraction |







Number Line:

Bead string:

-3

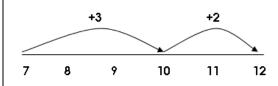
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10

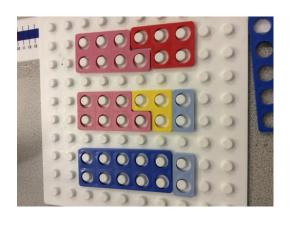
Counting up or 'Shop keepers' method

alongside the bead string, prior to transition to number line.

Number line



NUMICON

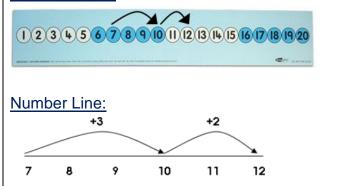


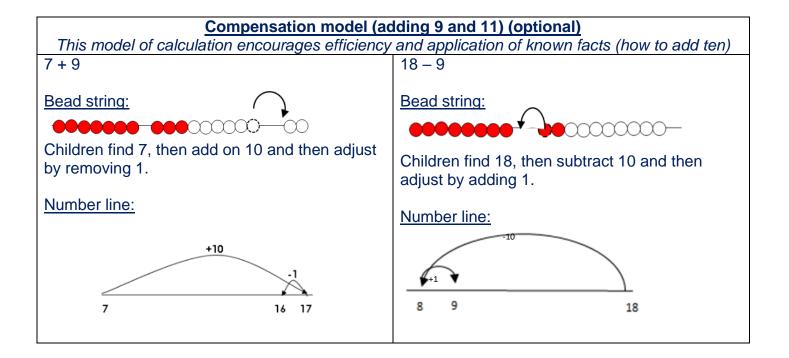
12 – 7 becomes 7 + 3 + 2. Starting from 7 on the bead string 'how many more to the next multiple of 10?' (children should recognise how their number bonds are being applied), 'how many more to get to 12?'. <u>Number Track:</u>

-2

11

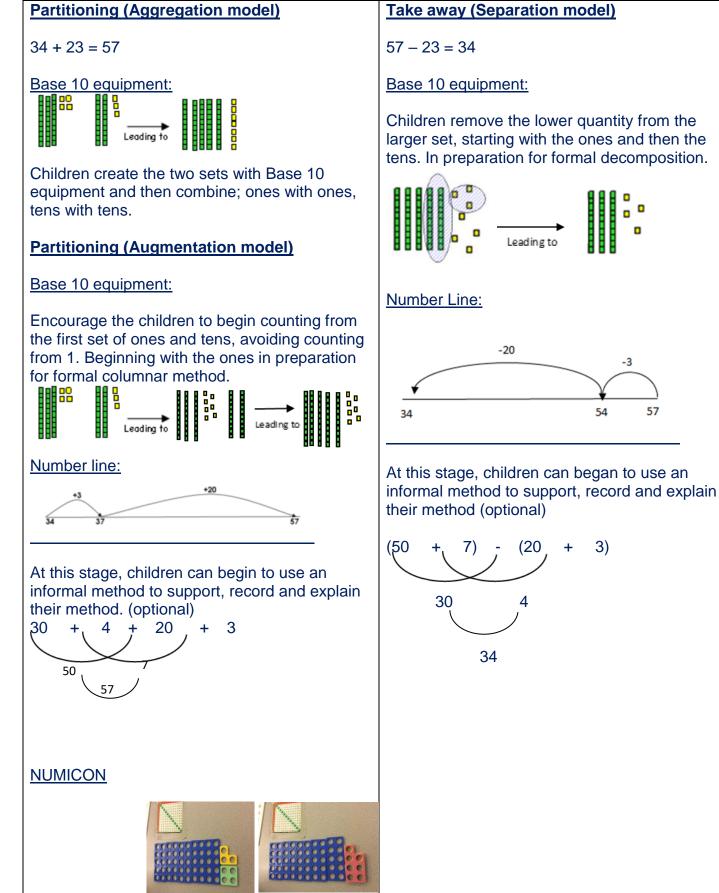
12



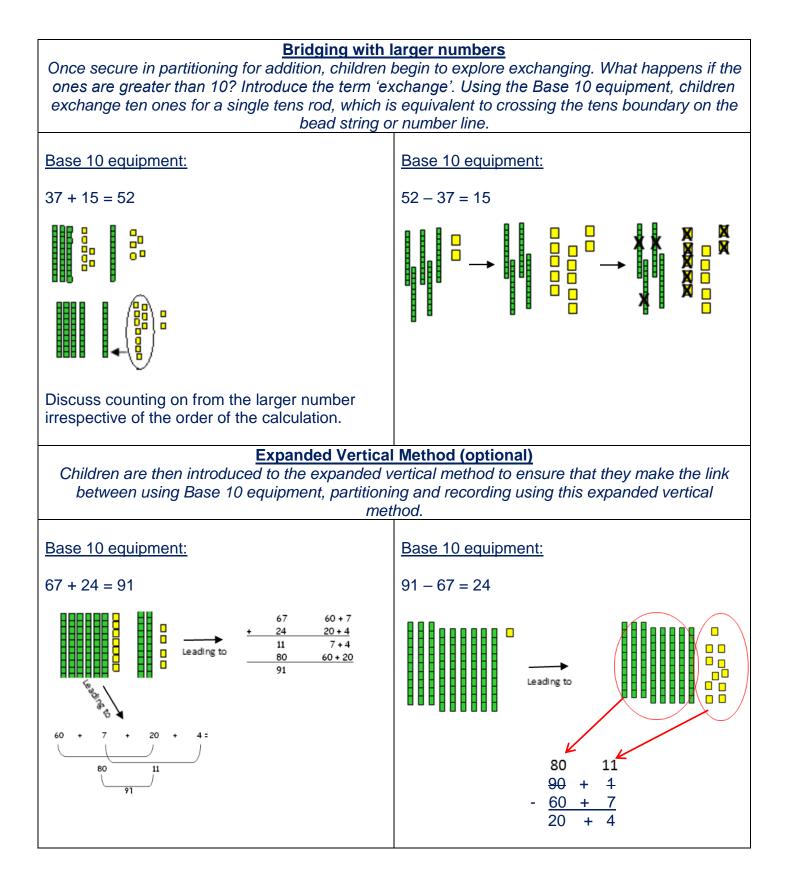


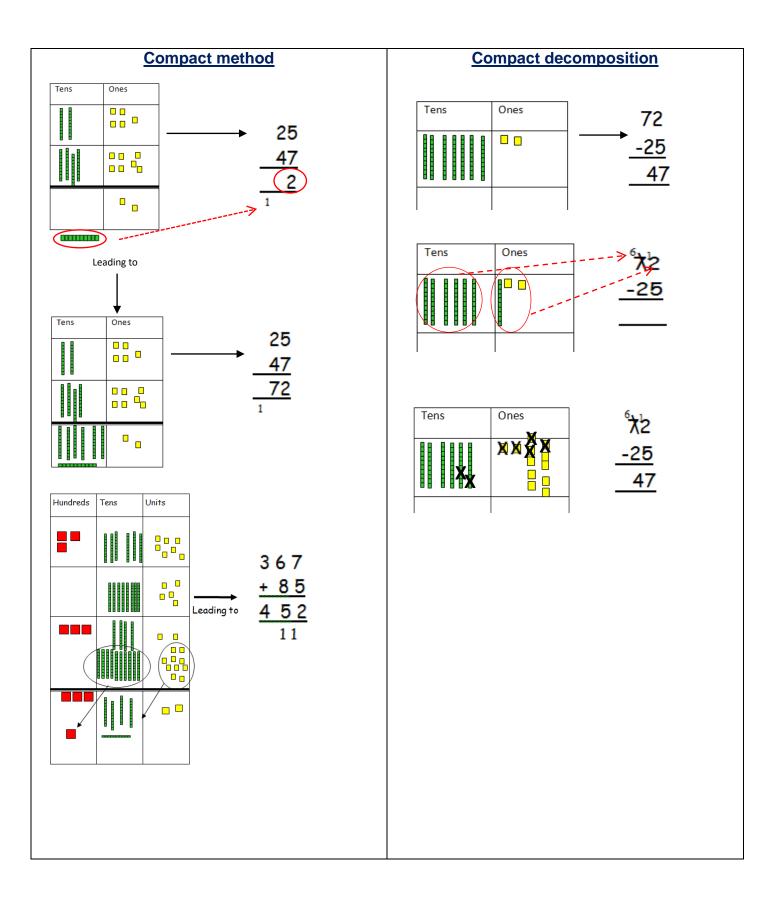
| Working with larger numbers | |
|-------------------------------|--|
| Tens and ones + tens and ones | |

Ensure that the children have been transitioned onto Base 10 equipment and understand the abstract nature of the single 'tens' sticks and 'hundreds' blocks

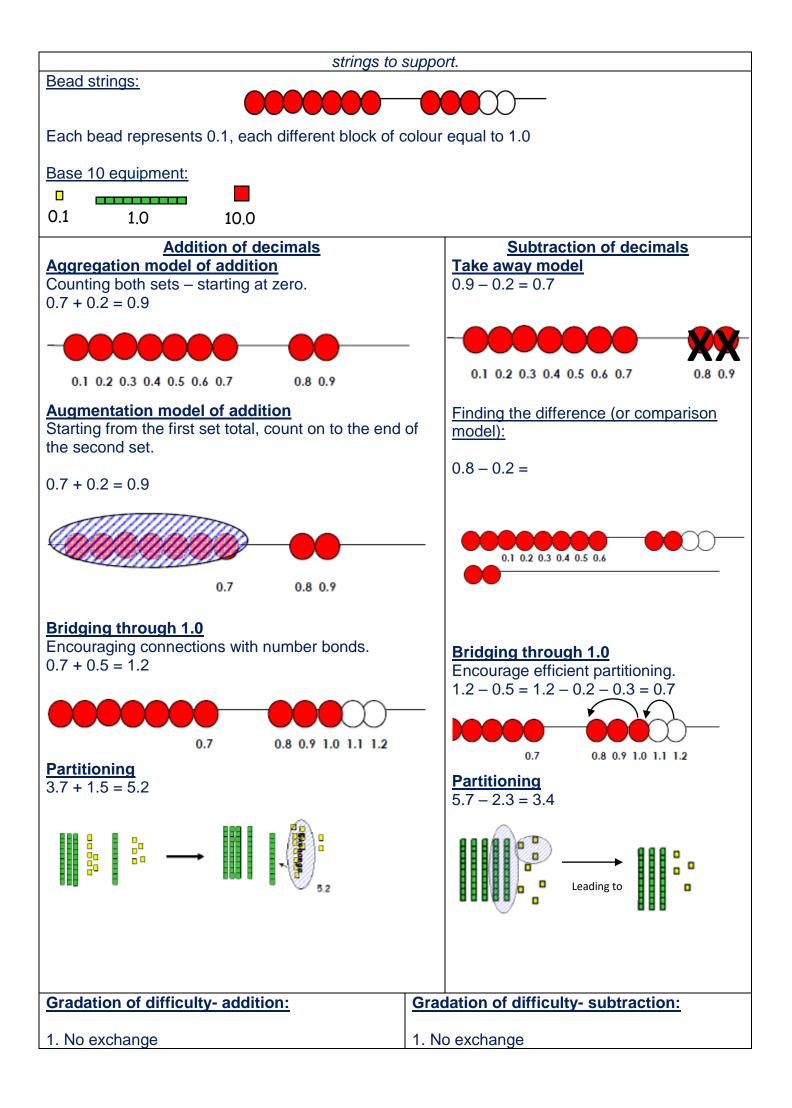


|--|--|--|





<u>Vertical acceleration</u> By returning to earlier manipulative experiences children are supported to make links across mathematics, encouraging 'If I know this…then I also know…' thinking. <u>Decimals</u> Ensure that children are confident in counting forwards and backwards in decimals – using bead



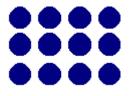
| 2. Extra digit in the answer | 2. Fewer digits in the answer |
|--|--|
| 3. Exchanging ones to tens | 3. Exchanging tens for ones |
| 4. Exchanging tens to hundreds | 4. Exchanging hundreds for tens |
| 5. Exchanging ones to tens and tens to hundreds | 5. Exchanging hundreds to tens and tens to ones |
| 6. More than two numbers in calculation | 6. As 5 but with different number of digits |
| 7. As 6 but with different number of digits8. Decimals up to 2 decimal places (same | 7. Decimals up to 2 decimal places (same number of decimal places) |
| number of decimal places) | 8. Subtract two or more decimals with a range of decimal places |
| 9. Add two or more decimals with a range of decimal places | |

Progression in Multiplication and Division

Multiplication and division are connected.

Both express the relationship between a number of equal parts and the whole.

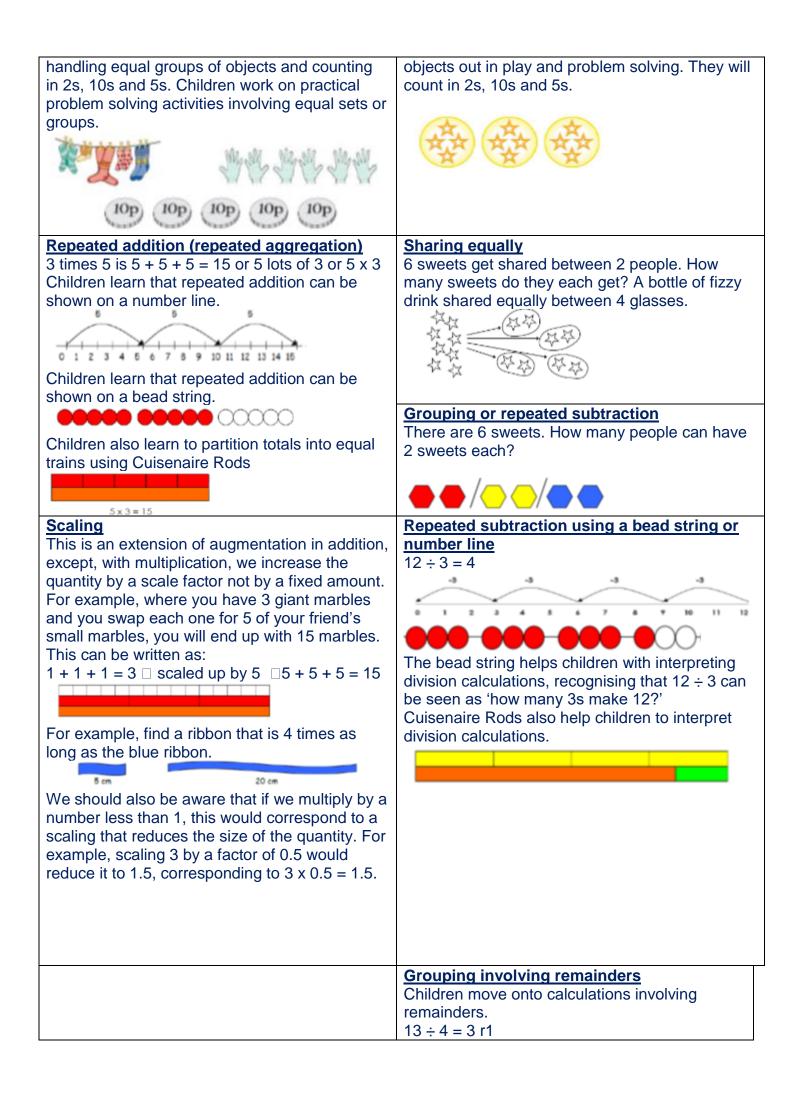
| Part | Part | Part | Part |
|-------|------|------|------|
| Whole | | | |

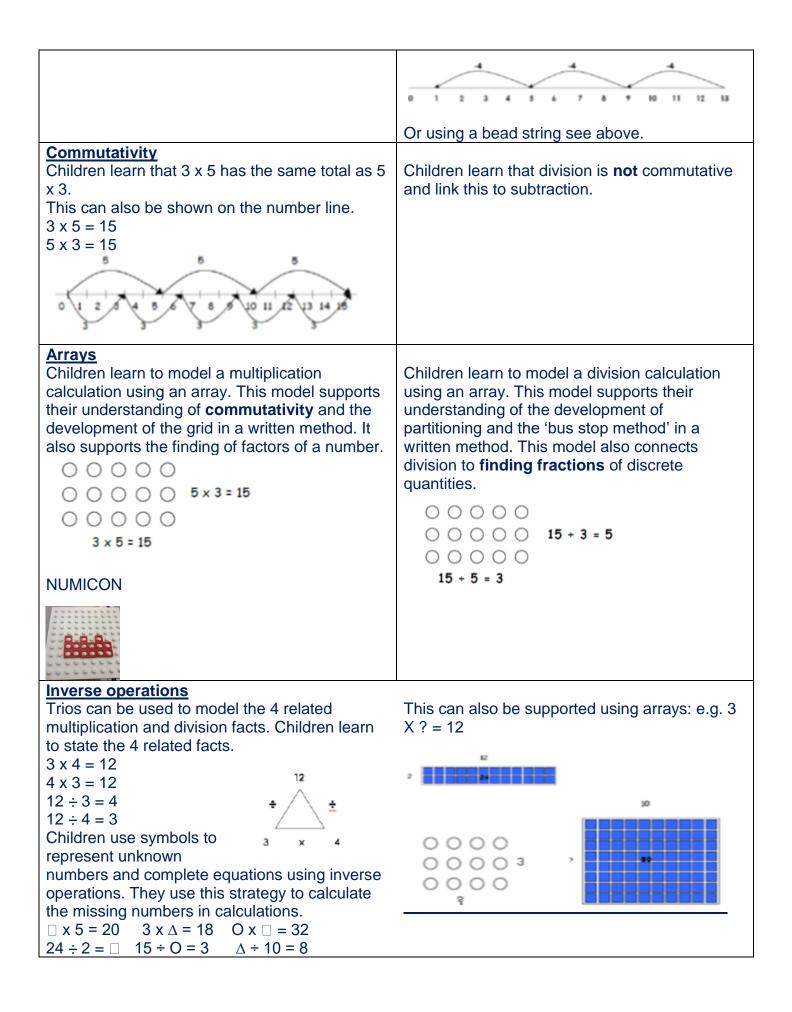


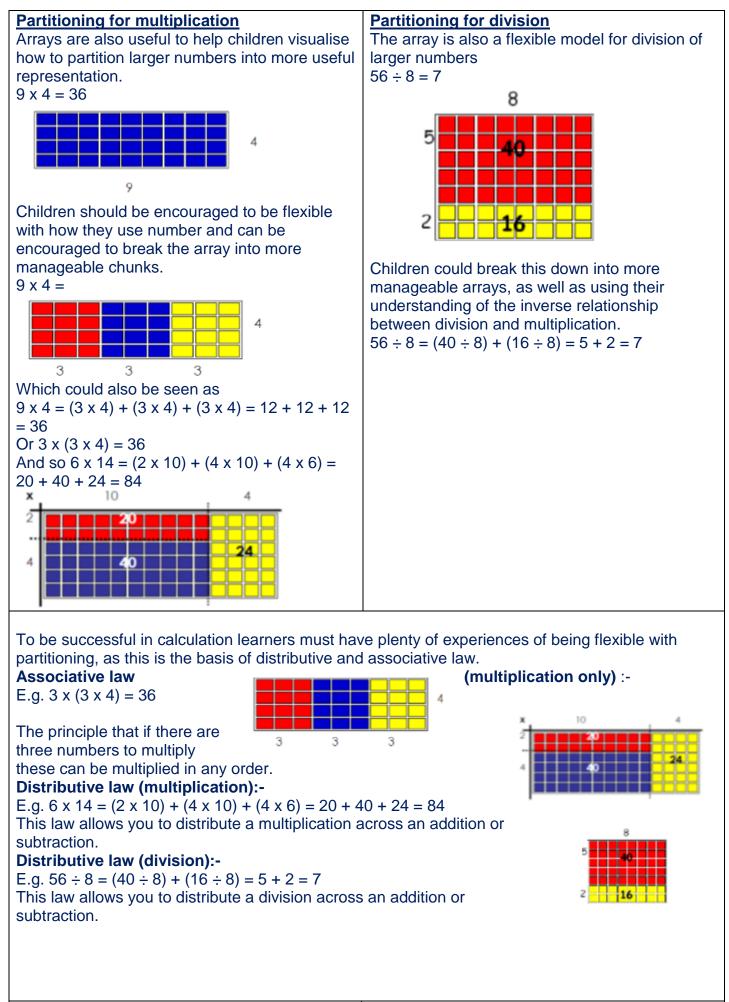
The following array, consisting of four columns and three rows, could be used to represent the number sentences: -

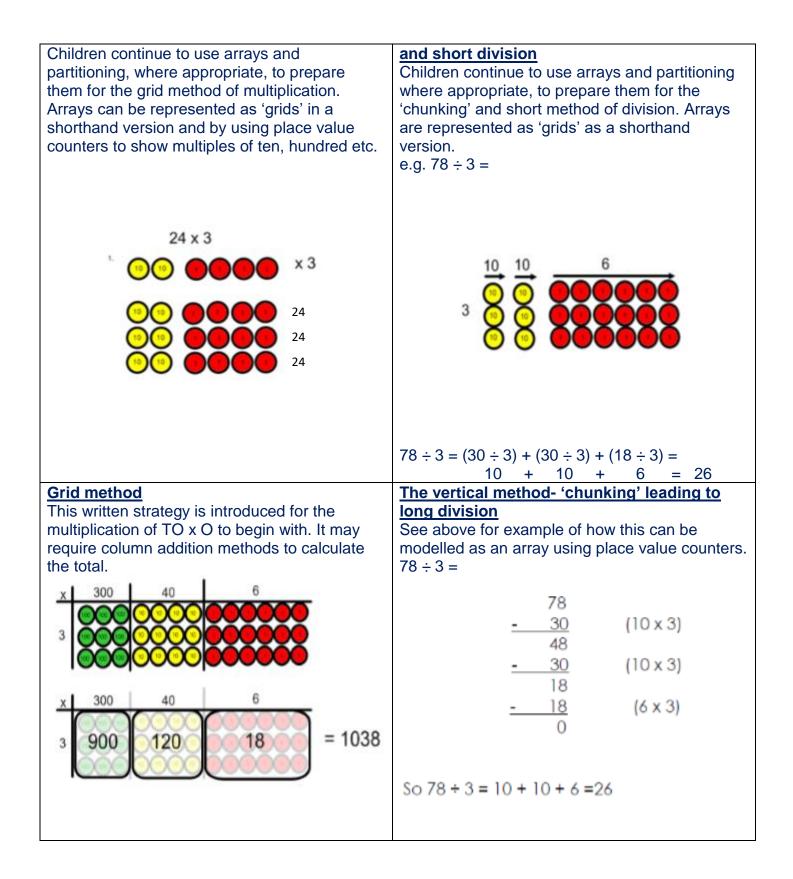
 $3 \times 4 = 12$, $4 \times 3 = 12$, 3 + 3 + 3 + 3 = 12, 4 + 4 + 4 = 12. And it is also a model for division $12 \div 4 = 3$ $12 \div 3 = 4$ 12 - 4 - 4 - 4 = 012 - 3 - 3 - 3 - 3 = 0

| Multiplication | Division |
|---|---|
| Early experiences | |
| Children will have real, practical experiences of | Children will understand equal groups and share |



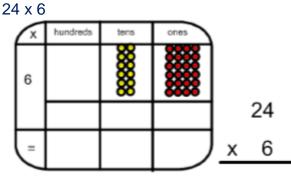


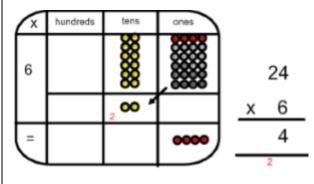


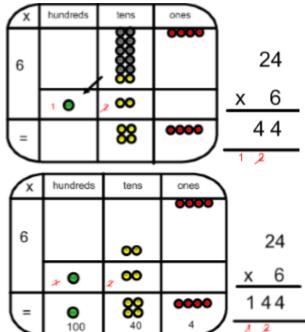


single digit

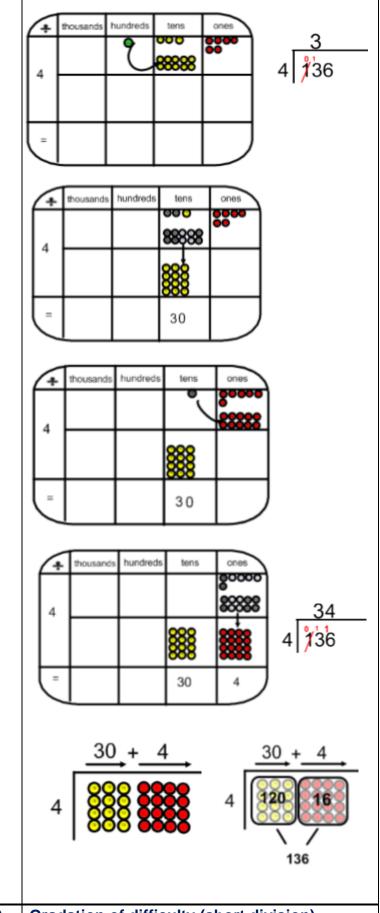
The array using place value counters becomes the basis for understanding short multiplication first without exchange before moving onto exchanging







Whereas we can begin to group counters into an array to show short division working $136 \div 4$



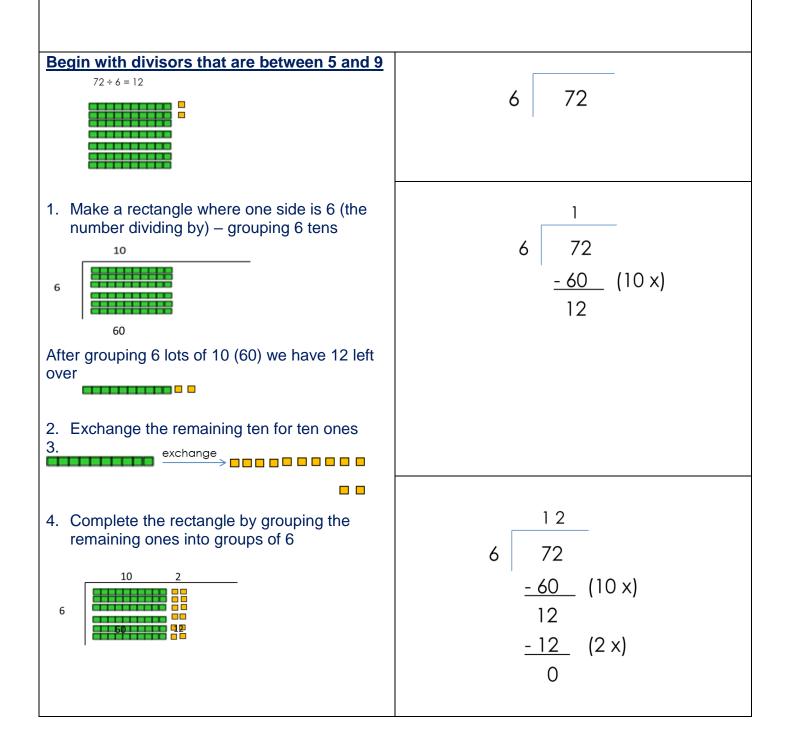
Gradation of difficulty (short multiplication)

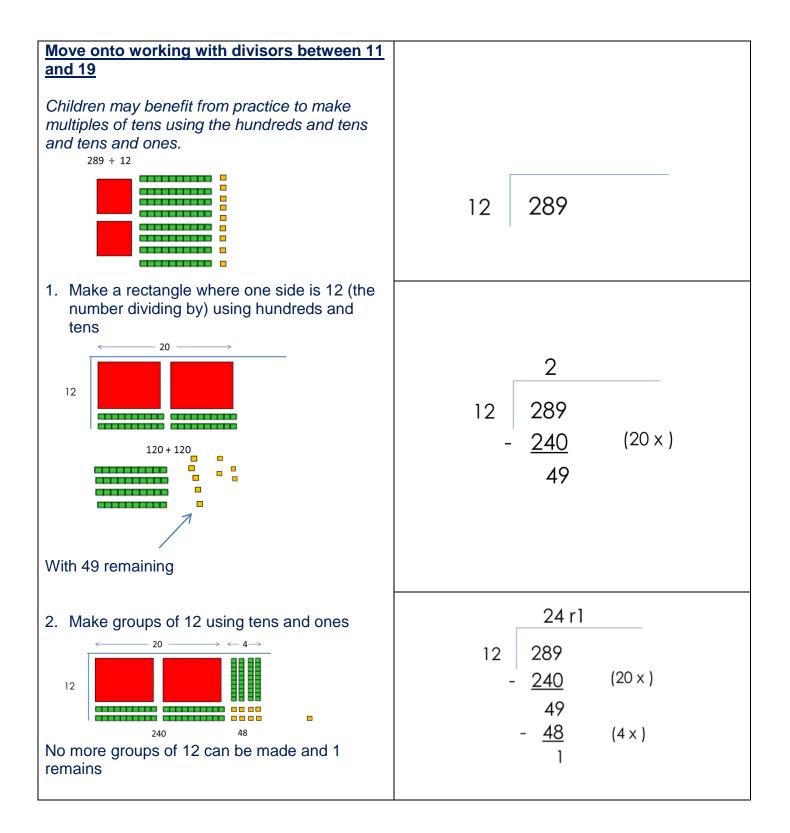
Gradation of difficulty (short division)

| 1. TO x O no exchange | 1. TO ÷ O no exchange no remainder |
|---|---|
| 2. TO x O extra digit in the answer | 2. TO ÷ O no exchange with remainder |
| 3. TO x O with exchange of ones into tens | 3. TO ÷ O with exchange no remainder |
| 4. HTO x O no exchange | 4. TO ÷ O with exchange, with remainder |
| 5. HTO x O with exchange of ones into tens | 5. Zero in the quotient e.g. $816 \div 4 = 204$ |
| 6. HTO x O with exchange of tens into hundreds | 6. As 1-5 HTO ÷ O |
| 7. HTO x O with exchange of ones into tens and tens into hundreds | 7. As 1-5 greater number of digits ÷ O |
| 8. As 4-7 but with greater number digits x O | 8. As 1-5 with a decimal dividend e.g. $7.5 \div 5$ or $0.12 \div 3$ |
| 9. O.t x O no exchange | 9. Where the divisor is a two digit number |
| 10. O.t with exchange of tenths to ones | Cashalaw far anadatian of difficulty with |
| 11. As 9 - 10 but with greater number of digits which may include a range of decimal places x O | See below for gradation of difficulty with remainders |
| | Dealing with remainders |
| | Remainders should be given as integers, but children need to be able to decide what to do after division, such as rounding up or down accordingly. e.g.: I have 62p. How many 8p sweets can I buy? Apples are packed in boxes of 8. There are 86 apples. How many boxes are needed? Gradation of difficulty for expressing remainders Whole number remainder Remainder expressed as a fraction of the divisor Remainder expressed as a simplified fraction |
| | 4. Remainder expressed as a decimal |
| Long multiplication—multiplying by more than one digit Children will refer back to grid method by using place value counters or Base 10 equipment with no exchange and using synchronised modelling of written recording as a long multiplication model before moving to TO x TO etc. | Long division —dividing by more than one digit Children should be reminded about partitioning numbers into multiples of 10, 100 etc. before recording as either:- 1. Chunking model of long division using Base 10 equipment 2. Sharing model of long division using place value counters See the following pages for exemplification of these methods. |
| Chunking model of long division using Base 1 | |
| This model links strongly to the array representation; so for the calculation $72 \div 6 = ?$ - one side of the array is unknown and by arranging the Base 10 equipment to make the array we can discover | |

?

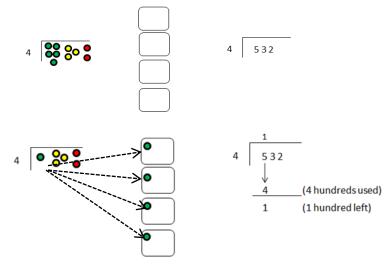
this unknown. The written method should be written alongside the equipment so that children make links.



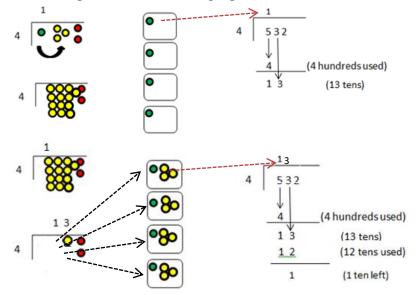


Sharing model of long division using place value counters

Starting with the most significant digit, share the hundreds. The writing in brackets is for verbal



Moving to tens - exchanging hundreds for tens means that we now have a total of 13 tens



Moving to ones, exchange tens to ones means that we now have a total of 12 ones counters (hence the arrow)

